

$$f(x) = \begin{cases} 0; & x \leq 0 \\ Ax; & 0 < x \leq 1 \\ 0; & x > 1 \end{cases} \quad \int_{-\infty}^{+\infty} f(x) dx = 1$$

$$\int_{-\infty}^{+\infty} f(x) dx = \int_{-\infty}^0 f(x) dx + \int_0^1 f(x) dx + \int_1^{+\infty} f(x) dx = \int_{-\infty}^0 0 * dx + \int_0^1 Ax * dx + \int_1^{+\infty} 0 * dx = 0 + \frac{Ax^2}{2} \Big|_{x=0}^1 + 0 = \frac{A * 1^2}{2} - \frac{A * 0^2}{2} = \frac{A}{2} = 1$$

$$A = 2$$

$$f(x) = \begin{cases} 0; & x \leq 0 \\ 2x; & 0 < x \leq 1 \\ 0; & x > 1 \end{cases}$$

$$F(x) = \int_{-\infty}^x f(t) dt = \begin{cases} \int_{-\infty}^x f(t) dt; & x \leq 0 \\ \int_{-\infty}^0 f(t) dt + \int_0^x f(t) dt; & 0 < x \leq 1 \\ \int_{-\infty}^0 f(t) dt + \int_0^1 f(t) dt + \int_1^x f(t) dt; & x > 1 \end{cases} = \begin{cases} \int_{-\infty}^x 0 * dt; & x \leq 0 \\ \int_{-\infty}^0 0 * dt + \int_0^x 2t * dt; & 0 < x \leq 1 \\ \int_{-\infty}^0 0 * dt + \int_0^1 2t * dt + \int_1^x 0 * dt; & x > 1 \end{cases} = \begin{cases} 0; & x \leq 0 \\ t^2 \Big|_{t=0}^x; & 0 < x \leq 1 \\ 0 + t^2 \Big|_{t=0}^1 + 0; & x > 1 \end{cases}$$

$$F(x) = \begin{cases} 0; & x \leq 0 \\ x^2; & 0 < x \leq 1 \\ 0; & x > 1 \end{cases}$$

$$MX = M(x) = \int_{-\infty}^{+\infty} f(x) * x * dx = \int_{-\infty}^0 f(x) * x * dx + \int_0^1 f(x) * x * dx + \int_1^{+\infty} f(x) * x * dx$$

$$MX = \int_{-\infty}^0 0 * x * dx + \int_0^1 2x * x * dx + \int_1^{+\infty} 0 * x * dx = 0 + \frac{2x^3}{3} \Big|_{x=0}^1 + 0 = \frac{2}{3}$$

$$DX = M\left((x - MX)^2\right) = \int_{-\infty}^{+\infty} f(x) * \left(x - \frac{2}{3}\right)^2 * dx = \int_{-\infty}^0 f(x) * \left(x - \frac{2}{3}\right)^2 * dx + \int_0^1 f(x) * \left(x - \frac{2}{3}\right)^2 * dx + \int_1^{+\infty} f(x) * \left(x - \frac{2}{3}\right)^2 * dx =$$

$$DX = \int_{-\infty}^0 0 * \left(x - \frac{2}{3}\right)^2 * dx + \int_0^1 2x * \left(x - \frac{2}{3}\right)^2 * dx + \int_1^{+\infty} 0 * \left(x - \frac{2}{3}\right)^2 * dx = 2 \int_0^1 \left(x - \frac{2}{3}\right) * \left(x - \frac{2}{3}\right)^2 * dx + 2 \int_0^1 \frac{2}{3} * \left(x - \frac{2}{3}\right)^2 * dx =$$

$$DX = \frac{2}{4} \left(x - \frac{2}{3}\right)^4 \Big|_{x=0}^1 + \frac{4}{3 * 3} \left(x - \frac{2}{3}\right)^3 \Big|_{x=0}^1 = \frac{1}{2} \left(\left(1 - \frac{2}{3}\right)^4 - \left(0 - \frac{2}{3}\right)^4 \right) + \frac{4}{9} \left(\left(1 - \frac{2}{3}\right)^3 - \left(0 - \frac{2}{3}\right)^3 \right) =$$

$$DX = \frac{1}{2} \left(\left(\frac{1}{3}\right)^4 - \left(\frac{2}{3}\right)^4 \right) + \frac{4}{9} \left(\left(\frac{1}{3}\right)^3 + \left(\frac{2}{3}\right)^3 \right) = \frac{1}{2} \left(\frac{1}{81} - \frac{16}{81} \right) + \frac{4}{9} \left(\frac{1}{27} + \frac{8}{27} \right) = -\frac{15}{2 * 81} + \frac{4}{27} =$$

$$DX = -\frac{5}{2 * 27} + \frac{4}{27} = \frac{4 * 2 - 5}{2 * 27} = \frac{3}{2 * 27} = \frac{1}{18}$$

$$p(x \in [a; b]) = \int_a^b f(x) dx$$

$$a = 0; b = 2$$

$$p(x \in [0; 2]) = \int_0^2 f(x) dx = \int_0^1 f(x) dx + \int_1^2 f(x) dx = \int_0^1 2x * dx + \int_1^2 0 * dx = x^2 \Big|_{x=0}^1 + 0 = 1$$